

Sixth Semester B.E. Degree Examination, Dec.2013/Jan.2014 Operations Research

Time: 3 hrs. Max. Marks: 100

Note: Answer FIVE full questions, selecting at least TWO questions from each part.

PART - A

- a. What is operation research? Mention six phases of an operation research study. (05 Marks)
 - b. A manufacturer produces three models I, II, III of certain product using raw materials A and B. The following table gives the data for the problem formulate the LP model:

Raw material	Requirement per unit			Availability
	I	II	III	
A	2	3	5	4000
B	4	2	7	6000
Min demand	200	200	150	-
Profit per unit (Rs.)	30	20	50	-

(05 Marks)

- c. Define:
 - i) Feasible solution
 - ii) Feasible region
 - iii) Optimal solution
 - iv) Degeneracy
 - v) Infeasible solution.

(10 Marks)

a. Define slack and surplus variables.

(04 Marks)

b. Find all the basic solutions of the following system of equation identifying in each case the basic and non basic variables:

$$2x_1 + x_2 + 4x_3 = 11$$

$$3x_1 + x_2 + 5x_3 = 14$$

(06 Marks)

c. Solve the following LPP using simplex method in tabular form:

Maximize $Z = 5x_1 + 3x_2$

Subject to,
$$x_1 + x_2 \le 2$$

$$5x_1 + 2x_2 \le 10$$

$$3x_1 + 8x_2 \le 12$$

$$x_1, x_2 \ge 0$$

(10 Marks)

3 a. Express the following LPP in canonical form

Maximize $Z = 2x_1 + 3x_2 + x_3$

Subject to,
$$4x_1 - 3x_2 + x_3 \le 6$$

$$x_1 + 5x_2 - 7x_3 \ge -4$$

$$x_1, x_2 \ge 0$$

(06 Marks)

b. Explain the computational steps of Big-M method.

(04 Marks)

c. Solve by Big-M method

Minimize
$$Z = 4x_1 + x_2$$

Subject to,
$$3x_1 + x_2 = 3$$

$$4x_1 + 3x_2 \ge 6$$

$$x_1 + 3x_2 \le 3$$

$$x_1, x_2 \ge 0$$
.

(10 Marks)

4 a. Use two phase method to minimize

$$5x_1 - 6x_2 - 7x_3$$
Subject to, $x_1 + 5x_2 - 3x_3 \ge 15$

$$5x_1 - 6x_2 + 10x_3 \le 20$$

$$x_1 + x_2 + x_3 = 5$$

$$x_1, x_2, x_3 \ge 0$$

(10 Marks)

b. Brief out the important characteristics of duality.

(04 Marks)

c. Construct the dual of an LPP

Minimize
$$Z = 3x_1 - 2x_2 - x_3$$

Subject to, $2x_1 + 3x_2 + x_3 \le 15$
 $4x_1 - 2x_2 \ge 9$
 $-8x_1 + 4x_2 + 3x_3 = 8$

(06 Marks)

PART - B

5 a. Solve by dual simplex method

$$Minimize Z = 2x_1 + x_2$$

Subject to,
$$3x_1 + x_2 \le 3$$

$$4x_1 + 3x_2 \ge 6$$

 $x_1, x_2, x_3 \ge 0.$

$$\mathbf{x}_1 + 2\mathbf{x}_2 \ge 3$$

$$\mathbf{x}_1, \mathbf{x}_2 \ge 0$$

(12 Marks)

b. Explain parametric integer linear programming and its significance. (08 Marks)

6 a. A dairy farm has 3 plants located at 3 different places and daily milk production of each plant is given as follows:

Plant	Production (in million ltrs)
1	6
2	1
3	10

Each day the firm must fulfill the needs of its 4 destination centres. Minimum requirement of each centre is as follows:

Centres	Requirement (million ltrs)
1	7
2	5
3	3
4	4

Cost of shipping 1 million ltr of milk from each plant of each centre is given in the below table

Formulate the LP model.

(10 Marks)

b. Solve the following transportation problem by North West corner rule and find the optimal solution:

(10 Marks)

	15	26	3	350
I	3	7	8	100
Į	9	4	3	110
	80	150	330	

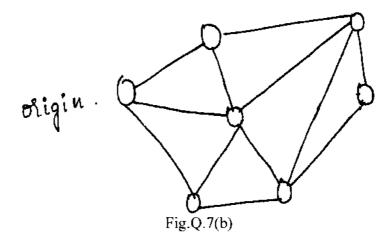
7 a. Find the optimality assignment for the following matrix:

(10 Marks)

	Α	В	C	D
1	2	3	4	5
2	4	5	6	7
3	7	8	9	8
4	3	5	8	4

b. Cable operator is planning to give cable network connections to six housing blocks shown below. The distances are given in hundreds of meters. Give optimum connection details.

(05 Marks)



c. Solve the following game:

	$\mathbf{B}_{\mathbf{l}}$	\mathbf{B}_2
A_1	-7	6
\mathbf{A}_2	7	-4
\mathbf{A}_3	-4	-2
A_4	8	-6

(05 Marks)

8 a. Explain the nature of meta heuristics.

(05 Marks)

b. Write a note on solving a non-linear programming problem. Explain tabu search.

(10 Marks)

c. Explain the outline of a basic genetic algorithm.

(05 Marks)

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